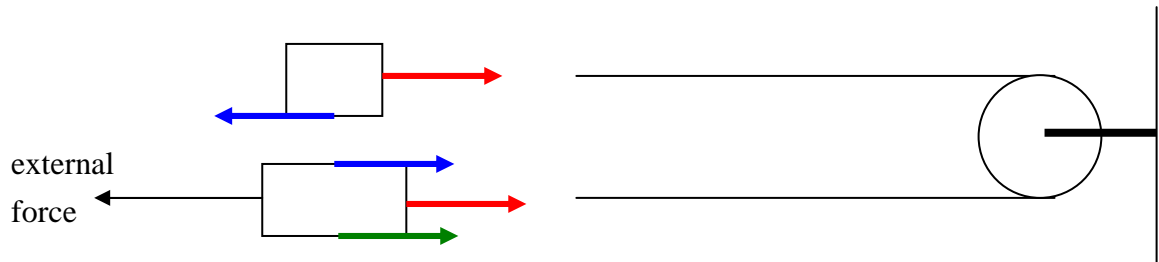


1997MC(1)



Red force: tension = T (along the same string, tension is unchanged)

Blue force = friction between the two blocks = fr

- the upper block tends to move to the right, so the friction on it is to the left
- by action and reaction, the friction on the lower block is to the right

Green force = friction between the lower block and the floor = fr'

The upper block is stationary, so $T = fr$

The lower block is stationary, so the external force = $T + fr + fr' = 2fr + fr'$

The frictional forces increase with the external force, keeping the blocks stationary, until they reach their maximum value, i.e. 2 N.

Therefore, the lower block starts to move when external force = $(2fr + fr')_{\text{maximum}} = 2 \times 2 + 2 = 6 \text{ N}$

1997MC (2)

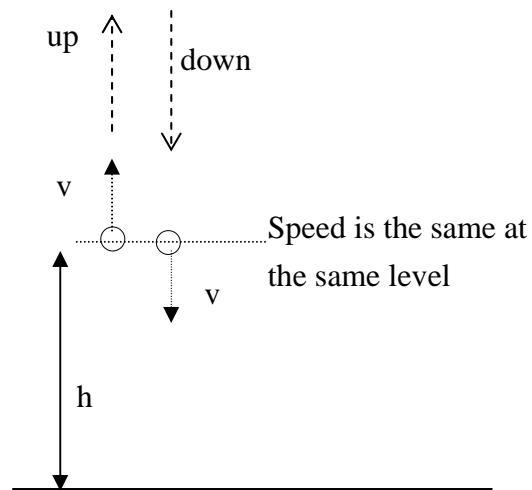
Total energy before reaching the ground = $mgh + mv^2/2$ (1)

Total energy after rebound = mgh (2)

(1) Correct, because there is energy loss during the rebound

(2) Correct. Energy loss = (1) – (2)

(3) Incorrect,



1997MC(3)

Let h be the height of the table

By conservation of energy

$$\frac{1}{2}mu^2 + mgh = \frac{1}{2}mv^2, \text{ so}$$

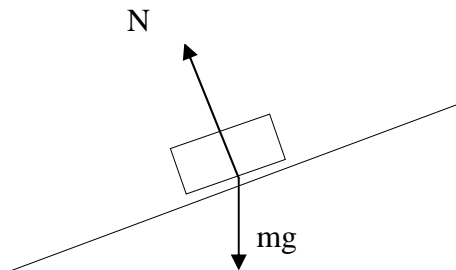
$$h = \frac{v^2 - u^2}{2g} \dots\dots\dots(1)$$

Vertical motion $h = \frac{1}{2}gt^2$

$$t = \sqrt{\frac{2h}{g}} \dots\dots\dots(2)$$

Putting (1) into (2), we will get the answer.

1997MC (4).



The acceleration is horizontal, so upward force = downward force

$$N\cos\theta = mg \dots\dots\dots(1)$$

The centripetal force is provided by $N\sin\theta$, so $N\sin\theta = mv^2/R \dots\dots\dots(2)$

From (1) and (2), $\tan\theta = mv^2/Rg$

$$v = \sqrt{Rg \tan \theta} = 5.4ms^{-1}$$

[Remark: We do not say $N = mg \cos\theta$ and $a = g\sin\theta$, because NOW, **THE ACCELERATION IS HORIZONTAL, NOT PARALLEL TO THE PLANE**]

1997MC (5)

Let r be the radius of the loop.

KE at the top of the loop is $mg(h-2r)$, so the speed at the top of the loop $v = \sqrt{2g(h-2r)}$

Net force at the top $F = mg + R$, which is the centripetal force required.

$$mg + R = mv^2/r = 2mg(h - 2r)/r$$

So R increases linearly with h.

1997MC(6)

- (1) Incorrect. The two fragments should have the same magnitude of momentum

$$M_1 V_1 + M_2 V_2 = 0$$

- (2) Correct. Speed = P/m , so smaller mass, larger speed

- (4) Correct. By writing $KE = P^2/2m$, where p is the momentum. Smaller mass, larger KE

1997MC (9)

Basic facts about SHM:

a leads v by $\pi/2$

v leads x by $\pi/2$

- (1) correct (2) correct (3) incorrect, because a and x are in anti-phase

1997MC (12)

Reflection of a transverse wave from a denser medium : π change, that means the wave is inverted

Reflection of a transverse wave from a less dense medium: no change in shape

1997MC (14)

- (1) Doppler effect, so the frequency will change.

- (2) Longer distance, intensity is reduced, so amplitude is smaller

- (3) If “speed” refers to the speed of propagation of wave in air, O.K., it doesn’t change, but if “speed “ refers to the speed of sound relative to the men on the ship, it is changed

1997 MC(15)

- (1) Incorrect. Path difference $3000 \text{ nm}/400 \text{ nm} = 7.5 = 7 + 1/2$

It is the 8th dark fringe.

$m = 0 \rightarrow$ 1st dark fringe

$m = 1 \rightarrow$ 2nd dark fringe

so on

- (2) Incorrect. The fringe pattern is independent of the separation between the light source and the slits.

- (3) Correct. $3000/500 = 6$ (so P becomes a bright fringe)

1997MC (16)

Pipe A: wavelength of fundamental note = $4L_A$

Pipe B; wavelength of fundamental note = $2L_B$

Same fundamental note, so same wavelength, $4L_A = 2L_B$ $L_A:L_B = 1:2$

1997MC (17)

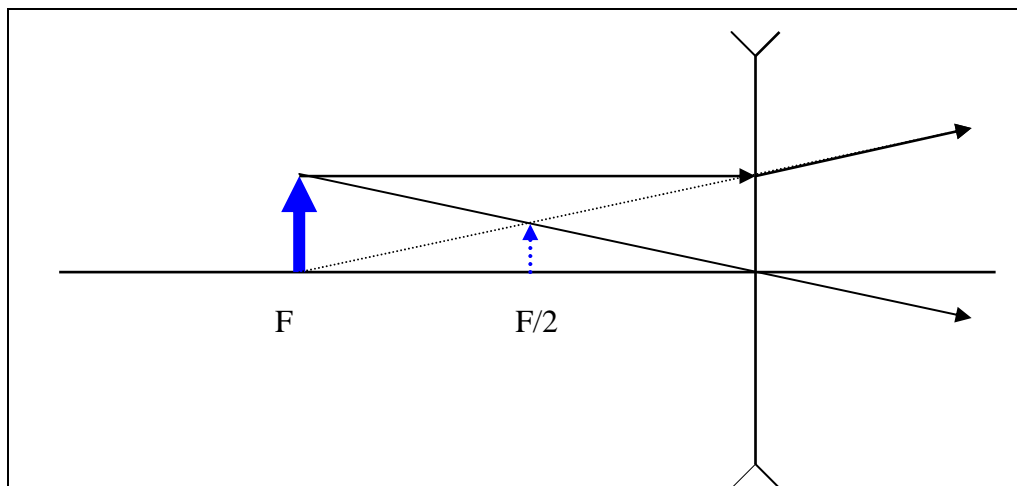
Optical path difference is increased if water is introduced (because wavelength is shorter in water).

For a particular order of fringe m , $2d = m\lambda$. After water is introduced, the condition becomes $2nd' = m\lambda$. Because $n > 1$, so $d' < d$. The same order now appears at a smaller thickness of film (i.e. at a smaller radius).

1997MC (18)

To a convex lens, object at $2F$, object is formed at $2F$, so to L_1 , $2f = 10$ cm, $f = 5$ cm

To a concave lens, object at F , image is formed at $F/2$



To L_2 , $f = 20$ cm > 10 cm

The best answer is D.

1997MC(19)

$$d \sin \theta = m\lambda$$

$$d \sin(90^\circ - 65^\circ) = \lambda \quad \dots\dots\dots(1)$$

[Note: θ is the angle measured from the zeroth order, which is 90° as measured by the protractor]

$$d \sin \theta = 2\lambda \quad \dots\dots\dots(2)$$

Divide (2) by (1) $\sin \theta = 2 \sin 25^\circ$

$$\theta = 58^\circ$$

The **protractor reads** $90^\circ - 58^\circ$ or $90^\circ + 58^\circ$

1997 MC(20)

Some facts about material

Stiffness (stiff/soft): slope of the elastic (linear) part

P is stiffer because it has a larger slope

Strength (strong/weak): highest point of the curve

Q has a greater strength because it has a higher ultimate tensile stress

Ductility (ductile/brittle): length of the plastic region

Q is more ductile because it has a longer plastic region

1997MC(21)

- (2)
- The number of conduction electrons per unit volume solely depends on the type of material.**

For instance, someone asks you: "There is a copper block of 1 m^3 , how many free electrons does it contain?" What will you do? You will use the molar mass of copper, Avogadro's constant, etc to calculate, rather than saying: "I can't calculate because I don't know what voltage is applying to the copper block"

Yes, $I = nqAv$, but it tells us nothing about what the quantity n really depends on.

Which of the four quantities n , q , A , and v is/are constant? We cannot tell from the equation itself. Only from the given information and other physics, we know n , q and A (assume same wire) are unchanged, so I is proportional to v .

Everybody knows density $\rho = \frac{M}{V}$, but would you say ρ is proportional to M ?

Another example is wave speed $v = f\lambda$. Would we say v is proportional to f ?

NO! " $v=f\lambda$ " is always true, but v may or may not depends on f (c.f. light in vacuum and light in glass)

" $y = kx$ " means y is proportional to x only when k is a constant

1997MC (24)

Volume control is usually a variable resistor

1997MC (25)

Mass is proportional to volume.

Length of X = 3(Length of Y)

Cross-sectional area of x = (Cross-sectional area of Y)/3 (because of same mass)

Resistance $R \propto \frac{l}{A}$ $R_X:R_Y = 9:1$

Power $P = I^2 R$ $P_X:P_Y = 9(1^2):1(2^2) = 9:4$

1997MC (26)

Basic facts about motor

Battery voltage = V , induced emf = ε , internal resistance = R

$$V - \varepsilon = IR$$

$$\varepsilon \propto \text{angular speed}$$

Power delivered by the battery = VI

Power loss in armature coil = I^2R

Mechanical power developed = $VI - I^2R = \varepsilon I$

1997MC (27)

- (1) Time constant of an RC circuit = RC , so the unit of RC is second.
- (2) Time constant of an LR circuit = L/R , so the unit of L/R is second.
- (3) Resonant frequency = $\frac{1}{\sqrt{LC}}$, so the unit of \sqrt{LC} is second (so LC is not)

1997MC (33)

- (1) The glass wall is in thermal equilibrium. Its temperature does not rise after reaching the equilibrium. Then, the glass wall does not gain a net energy.
- (2) No, if the resistance is high, the power of the lamp will be very small. This is irrelevant to the low efficiency of the lamp bulb.
- (3) Most of the energy is dissipated as thermal energy. The thermal energy is radiated to outside in the form of infra-red

1997MC (40)

$$\text{Total impedance } Z = \sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}$$

$$\text{RMS current (ammeter reading) } I_{\text{rms}} = V_{\text{rms}}/Z$$

As freq increases, Z decreases, so RMS current increases.

$$\text{RMS voltage across C (voltmeter reading)} = I_{\text{rms}} X_C$$

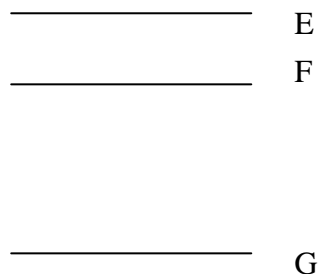
$$= \frac{V_{\text{rms}}}{\omega C \sqrt{R^2 + \left(\frac{1}{\omega C}\right)^2}} = \frac{V_{\text{rms}}}{\sqrt{(\omega CR)^2 + 1}}$$

When frequency increases, RMS voltage across C decreases.

[Quick thinking: a cap behaves as a “perfect conducting wire” at high frequencies, so as frequency increases, total current rises and the p.d. across C drops]

1997MC (41)

Suppose the three levels are E, F and G.



Longest wavelength of photon comes from the transition from E to F

$$h \frac{c}{\lambda_2} = E - F \dots\dots\dots(1)$$

Shortest wavelength of photon comes from the transition E to G

$$h \frac{c}{\lambda_1} = E - G \dots\dots\dots(2)$$

Let the wavelength of the photon originating from the transition is F to G be λ

$$h \frac{c}{\lambda} = F - G \dots\dots\dots(3)$$

Since $(3) = (2) - (1)$

$$\frac{1}{\lambda} = \frac{1}{\lambda_1} - \frac{1}{\lambda_2} \quad \text{or} \quad \lambda = \left(\frac{1}{\lambda_1} - \frac{1}{\lambda_2} \right)^{-1}$$

[If F is closer to G, the longest wavelength comes from F to G.. Nevertheless, the result is the same]

1997MC (42)

It is a summing amplifier

$R_f = 20\text{k}\Omega$.

Two input voltages to V.

$$\text{One input voltage: } V_1 = 30\left(\frac{2}{3}\right) - 15 = 5V \quad R_{i1} = 10\text{ k}\Omega$$

$$\text{The other input voltage: } V_2 = 30\left(\frac{1}{3}\right) - 15 = -5V \quad R_{i2} = 20\text{ k}\Omega$$

$$V_{\text{out}} = -R_f\left(\frac{V_1}{R_{i1}} + \frac{V_2}{R_{i2}}\right) = -5V$$

1997MC (43)

Let m α -particles and n β -particles are emitted

One α particle will decrease the mass number by 4.

$$226 - 206 = 4m \quad m = 5$$

One α particle decreases the atomic number by 2 and one β particle increases the atomic number by 1.

$$88 - 82 = m(2) - n \quad n = 4$$
